## Mathematical Economics

Final (partial) Examination June 7, 2017

*Please, answer the following 3 questions.* **Time allowed**: one hour and 30 minutes. *PLEASE PLEASE, make an effort to write in a legible and organized fashion.* 

**Question 4.** Upper and lower hemi-continuity. Definitions and examples. Relations with other properties (closed-, compact- and convex-valued, closed- and convex-graph). The maximum theorem.

Finally, consider the correspondence  $\varphi(x) : [0,3] \to \mathbb{R}$  defined by

$$\varphi(x) = \begin{cases} [0,1] & x \in [0,1] \\ [0.25,0.75] & x \in (1,2) \\ [0,1] & x \in [2,3] \end{cases}$$

Identify all the properties it satisfies.

**Question 5.** Articulate a finite-horizon dynamic programming problem, and discuss, in as much detail as possible, the structure of its optimal strategies (under natural assumptions on the structure of the problem).

**Question 6.** Articulate a stationary discounted dynamic programming (SDDP) problem and define an optimal strategy for such problem. Discuss the first basic assumption on the structure of the problem and explain, in as much detail as possible, which pathologies it is meant to exclude. Finally, after having defined the value function for the problem, recall the important property that the value function has to satisfy given the assumption discussed earlier, proving what you can. What is the role played by this property in the solution of SDDPs?