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Life-cycle welfare losses from rules-of-thumb asset allocation*

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1. Introduction

Workers usually delegate the task of managing their savings to pension funds and other long-term institutional investors. The latter often propose plans with a decreasing age profile of investment in the riskier assets, the equity share being often in excess of 80% when young. This practice approximates well the optimal asset allocation age profile obtained from standard life-cycle models of household portfolio choice (Cocco et al., 2005; Gomes and Michaelides, 2005; Gomes et al., 2008). In fact, the welfare loss incurred by agents who adopt popular investment "rules of thumb" instead of the optimal strategy is negligible, being equivalent to 0.2–0.8% of annual consumption. Importantly, those models do not allow for (possibly long-lasting) unemployment spells in the investor's working career.

This paper provides an assessment of the welfare loss associated with the use of simple investment rules when workers face

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ABSTRACT

How should workers invest over the life-cycle? Should they follow some typical prescriptions ("rules of thumb") in personal finance implying higher equity investments when young? We show that the answer hinges on the risk of long-term unemployment spells, entailing permanent declines in workers' future earnings prospects. Absent unemployment risk, extant prescriptions deliver portfolios that are close to optimal, implying negligible welfare losses. They instead lead to sizeable welfare losses (3%–9% of annual consumption) when the risk of human capital depreciation following long-term unemployment is considered and realistically calibrated to the U.S. labor market. These losses stem from excess risk taking when young investors face uncertainty about future labor and pension incomes. This result points to a new design for pension plans offered by long-term institutional investors.

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long-term unemployment risk, yielding permanent reductions of their earning prospects. Such depreciation of workers' human capital as a consequence of prolonged unemployment has been recently documented by, among others, Edin and Gustavsson (2008) and Schmieder et al. (2016); moreover, Kroft et al. (2016) show that this phenomenon is common to all education groups and most industries in the U.S. in the aftermath of the Great Recession episode. Following this lead, a recent strand of literature in household finance extends the basic life-cycle setup to the possibility that investors experience periods of (even long-term) unemployment (Bremus and Kuzin, 2014; Chang et al., 2018; Bagliano et al., 2019). However, none of those papers evaluate the welfare losses that investors incur should they not adopt the optimal portfolio allocation, following instead simpler rules of thumb.

The purpose of the present paper is to provide such welfare analysis, quantifying the loss due to the adoption of sub-optimal investment strategies in the presence of (realistically calibrated) long-term unemployment risk with permanent consequences on workers' human capital. We show that in this case the optimal age profile of stock investment is substantially different from the standard, decreasing with age, pattern: the equity share is lower for young workers and remarkably constant throughout working life and retirement. Consequently, the welfare loss associated with the adoption of simple rules of thumb is much larger (equivalent to 3%–9% of annual consumption), casting serious doubts on

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the appropriateness of popular financial advice on life-cycle asset allocation strategies.

The rest of the paper is organized as follows. In Section 2, we describe a life-cycle model which accounts for long-term unemployment risk and calibrate it to match U.S. evidence. In Section 3, we show and discuss the results on the optimal life-cycle profile of stock investment. Section 4 presents the welfare comparison of the optimal strategy with two very common suboptimal investment rules of thumb. Section 5 concludes.

2. A life-cycle model with long-term unemployment risk

We extend the standard model of life-cycle saving and portfolio allocation to allow for the possibility of long-term unemployment spells, entailing a deterioration of workers' human capital and therefore a permanent reduction of earning prospects.

2.1. The model

The investor maximizes the expected discounted utility of consumption over working life, starting at age t_0 , and retirement, which begins with certainty at age $t_0 + K$; she also wishes to leave a bequest. Life lasts at most *T* periods, and is governed by age-dependent life expectancy: at each date *t*, the survival probability of being alive at date t + 1 is p_t (with $p_{t_0-1} = 1$). Individual preferences are described by a time-separable power utility function:

$$U_{t_0} = E_{t_0} \left[\frac{C_{t_0}^{1-\gamma}}{1-\gamma} + \sum_{j=1}^{T} \beta^j \left(\prod_{k=-1}^{j-2} p_{t_0+k} \right) \times \left(p_{t_0+j-1} \frac{C_{t_0+j}^{1-\gamma}}{1-\gamma} + (1-p_{t_0+j-1}) b \frac{(X_{t_0+j}/b)^{1-\gamma}}{1-\gamma} \right) \right]$$
(1)

where C_t is consumption at time t, X_t is the amount of wealth (cash on hand) the investor leaves as a bequest if death occurs, $b \ge 0$ is a parameter capturing the strength of the bequest motive, $\beta < 1$ is a utility discount factor, and γ is the constant relative risk aversion parameter.

During working life individuals supply labor inelastically and receive exogenous stochastic earnings. Admittedly, these assumptions do not allow us to disentangle the effects of (various sources of) exogenous shocks from the effects of endogenous workers' reactions, as in Low et al. (2010). In our framework, we introduce long-term unemployment risk by modeling working careers as a Markov chain with three possible states: employment (e), short-term unemployment (u_1) and long-term unemployment (u_2), with the following transition matrix:

$$\Pi_{s_{t},s_{t+1}} = \begin{pmatrix} \pi_{ee} & \pi_{eu_{1}} & \pi_{eu_{2}} \\ \pi_{u_{1}e} & \pi_{u_{1}u_{1}} & \pi_{u_{1}u_{2}} \\ \pi_{u_{2}e} & \pi_{u_{2}u_{1}} & \pi_{u_{2}u_{2}} \end{pmatrix} = \begin{pmatrix} \pi_{ee} & 1 - \pi_{ee} & 0 \\ \pi_{u_{1}e} & 0 & 1 - \pi_{u_{1}e} \\ \pi_{u_{2}e} & 0 & 1 - \pi_{u_{2}e} \end{pmatrix}$$

$$(2)$$

where $\pi_{nm} = \operatorname{Prob}(s_{t+1} = n | s_t = m)$ with $n, m = e, u_1, u_2$. A worker employed at t ($s_t = e$) can continue her employment spell at t + 1 ($s_{t+1} = e$) with probability π_{ee} , or can enter short-term unemployment ($s_{t+1} = u_1$) with probability $\pi_{eu_1} = 1 - \pi_{ee}$. If short-term unemployed at t ($s_t = u_1$), she exits unemployment ($s_{t+1} = e$) with probability π_{u_1e} or becomes long-term unemployed ($s_{t+1} = u_2$) with probability $\pi_{u_1u_2} = 1 - \pi_{u_1e}$. Finally, if the worker is long-term unemployed at t ($s_t = u_2$), she is re-employed in the following period ($s_{t+1} = e$) with probability $\pi_{u_2u_2} = 1 - \pi_{u_2e}$.

In each period, an employed worker earns labor income Y_t driven by permanent and transitory shocks, as in Cocco et al. (2005). Y_t is generated by the following process:

$$Y_t = H_t U_t \qquad t_0 \le t \le t_0 + K \tag{3}$$

where $H_t = F(t, \mathbf{Z}_t) P_t$ represents the permanent income component. In particular, $F(t, \mathbf{Z}_t)$ captures the deterministic trend in income that depends on age (*t*) and a vector of individual characteristics (\mathbf{Z}_t) such as gender, marital status, household composition and education. The logarithm of the stochastic permanent component P_t is assumed to follow a random walk process:

$$\log P_t = \log P_{t-1} + \omega_t \tag{4}$$

where ω_t is distributed as $N(0, \sigma_{\omega}^2)$. Finally, U_t denotes the transitory stochastic component and $\varepsilon_t \equiv \log(U_t)$ is distributed as $N(0, \sigma_{\varepsilon}^2)$ and uncorrelated with ω_t .

We extend this standard specification of the income process by introducing the novelty that unemployment duration affects the permanent component of labor income: the longer the unemployment spell, the larger is the worker's human capital depreciation, causing a permanent decrease in expected future earnings. After one-period unemployment the permanent component of labor income H_t is equal to H_{t-1} eroded by a fraction Ψ_1 , and after a two-period unemployment H_t is reduced by a fraction $\Psi_2 > \Psi_1$. Thus, permanent labor income evolves according to

$$H_{t} = \begin{cases} F_{t} P_{t} & \text{if } s_{t} = e \text{ and } s_{t-1} = e \\ (1 - \Psi_{1})H_{t-1} & \text{if } s_{t} = e \text{ and } s_{t-1} = u_{1} \\ (1 - \Psi_{2})H_{t-1} & \text{if } s_{t} = e \text{ and } s_{t-1} = u_{2} \end{cases} \qquad t = t_{0}, \dots, t_{0} + K$$
(5)

During unemployment, the worker receives unemployment benefits as a fixed proportion (ξ_1 and ξ_2 in the case of short-term and long-term unemployment, respectively) of her last working year labor income. Finally, as in the standard life-cycle model, during retirement the individual receives income equal to a fraction λ of the permanent labor income earned in her last working year.

During both working life and retirement, savings can be invested in a short-term riskless asset, yielding a constant gross real return R^f , and one risky asset ("stocks") yielding stochastic gross real returns R^s_t in each period. The excess returns of stocks is modeled as $R^s_t - R^f = \mu^s + \nu^s_t$, where μ^s is the expected stock premium and ν^s_t is a normally distributed innovation, with mean zero and variance σ^2_s .

Given uncertain labor income and asset returns, the investor maximizes expected discounted utility over her life span by choosing optimal consumption and portfolio allocation rules. We formulate her problem recursively by means of the following Bellman equation:

$$V_{t}(X_{t}, P_{t}, s_{t}) = \max_{C_{t}, \alpha_{t}^{S}} \frac{C_{t}^{1-\gamma}}{1-\gamma} + \beta \left[p_{t} \sum_{s_{t+1}=e, u_{1}, u_{2}} \pi (s_{t+1}|s_{t}) \widetilde{E_{t}} V_{t+1} \right. \\ \left. \times \left(X_{t+1}, P_{t+1}, s_{t+1} \right) \right. \\ \left. + (1-p_{t}) b \frac{(X_{t+1}/b)^{1-\gamma}}{1-\gamma} \right]$$
(6)

subject to $X_{t+1} = (X_t - C_t) (\alpha_t^s R_t^s + (1 - \alpha_t^s) R^f) + Y_{t+1}$, with α_{it}^s and $(1 - \alpha_t^s)$ denoting the shares of the investor's portfolio invested in stocks and in the riskless asset respectively.¹ In (6),

¹ We do not allow for short sales and we assume that the investor is liquidity constrained. Consequently, the amounts invested in stocks and in the riskless asset are non negative in all periods.

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 \overline{E}_t denotes the expectation operator taken with respect to continuous stochastic variables (ω_{t+1} , ε_{t+1} and ν_{t+1}^s), and π ($s_{t+1}|s_t$) are the entries of the transition matrix (2). We solve this problem by means of numerical techniques.²

2.2. Calibration

Calibration of the model requires choosing parameters of the investor's preferences, labor and retirement incomes, and the moments of stock returns. In order to focus on the role of long-term unemployment risk in shaping optimal life-cycle portfolio allocation, we adopt, wherever possible, the calibration in Cocco et al. (2005), a standard benchmark in the literature.

Table 1 collects the values of the key parameters of the model, calibrated to the U.S. economy, with source references. In what follows we comment on our main choices. The investor's working life spans (at most) 45 periods, from the age of 20 up to 65, when retirement occurs. After retirement, she can live for a maximum of 35 periods until the age of 100.³ As for preferences, we set the coefficient of relative risk aversion $\gamma = 5$, as in Chang et al. (2018), much lower than the value typically adopted in the literature.⁴ The riskless rate is fixed at 2% and the expected equity premium μ^{s} at 4%, with stock returns innovations, uncorrelated with permanent labor income shocks, displaying a variance set at 0.025. The labor income process is calibrated using the estimated parameters for U.S. households with high school education (but not a college degree) in Cocco et al. (2005).⁵ After retirement, income is a constant proportion λ of the final (permanent) labor income, set at 0.68, as the net replacement rate of total pension benefits for the average earner in the U.S. (OECD, 2015).

In our model workers bear the risk of (possibly persistent) unemployment. The annual transition probabilities among labor market states (employment, short-term unemployment and long-term unemployment) are chosen to match the average unemployment rate experienced by the U.S. in recent years. In particular, using data from the Current Population Survey (CPS) reported by Kroft et al. (2016), we calibrate the annual transition probability from employment to (short-term) unemployment at 4% and the probability of leaving unemployment after the first year at 85%. Finally, we set the probability of transition from long-term unemployment to employment at 33% in order to yield unconditional probabilities of being short-term and long-term unemployed matching our U.S. post-Great Recession target. The resulting annual transition matrix

$$\Pi_{s_t, s_{t+1}} = \begin{pmatrix} 0.96 & 0.04 & 0\\ 0.85 & 0 & 0.15\\ 0.33 & 0 & 0.67 \end{pmatrix}$$
(7)

delivers unconditional probabilities of being short-run (3.8%) and long-run unemployed (1.7%) in line with the overall (5.5%) and

long-term (1.7%) unemployment rates occurred in the U.S. in 2015.

Moreover, long unemployment spells entail a loss in the worker's expected permanent earnings due to human capital depreciation as shown in (5). We base our calibration of the effects of protracted inactivity on job careers on the evidence provided by Jacobson et al. (2005), who estimate that average earnings losses for displaced workers amount to 43-66% of their predisplacement wage, and by Guevenen et al. (2017), who find that the median earnings loss after a full year nonemployment amounts to 50% of previous income. Other studies document smaller earning losses, varying from 15% (Couch and Placzek, 2010) to about 25% (Jacobson et al., 1993) of predisplacement levels. Given the wide range of estimates of earning losses, we make a rather conservative choice, setting $\Psi_1 = 0$ (no loss for short-term unemployed) and $\Psi_2 = 0.25$, implying a 25% reduction of the permanent labor income component from the second year of unemployment.

Finally, unemployment benefits are calibrated according to the U.S. unemployment insurance system (OECD, 2010). Considering that the replacement rate with respect to last labor income is on average low and state benefits are paid for a maximum of 26 weeks, we set $\xi_1 = 0.3$ in case of short-term unemployment spells and a smaller value of $\xi_2 = 0.1$ for the long-term unemployed.

3. Results

Solving the model with the parameters displayed in Table 1 yields optimal policy functions for consumption and the portfolio share invested in stocks.⁶ Using those functions we simulate the whole life-cycle consumption and portfolio allocation decisions of a very large number of individuals (200.000) who start working at age 20 and face the realizations of shocks to labor income and stock returns drawn from the stochastic processes with parameter values reported in Table 1. In each period, the evolution of workers' employment status is driven by the transition probabilities in (7).

Fig. 1 shows the median of the distribution of investors' optimal risky portfolio share along the life cycle. As a benchmark for comparison, the Figure also displays the corresponding life-cycle profile obtained from solving and simulating the model without unemployment risk. The latter scenario is obtained by setting $\pi_{ee} = 1$ and all other entries equal to 0 in (2) and corresponds to the standard life-cycle set-up in Cocco et al. (2005).

In the case of no unemployment risk, the typical result on the age profile of the optimal stock portfolio share is obtained: the median investment in stocks is 100% during most of the working life and then decreases with age to reach around 75% at retirement and thereafter. The reason why investors should reduce exposure to risky assets as they approach retirement is that human capital provides a hedge against shocks to stock returns, making financial risk bearing more attractive. In early and middle stages of working life, when human capital is large relative to accumulated financial wealth, investment in stocks should be high; as retirement approaches human capital decreases relative to financial wealth and the portfolio should be rebalanced towards less risky assets.

When long-term unemployment risk is introduced, entailing rare but permanent declines in future earnings, the optimal stock share is sizably reduced at any age and almost flat at around 60%, as Fig. 1 shows. In this setting, human capital is lower and riskier, particularly for younger workers, inducing lower stock

 $^{^2\,}$ Details on the solution procedure are reported in the online Appendix A, where we also show how the evolution of the permanent component of labor income depends on previous individual labor market dynamics.

³ In each period, we take the conditional probability of being alive in the next period p_t from the life expectancy tables of the U.S. National Center for Health Statistics.

⁴ Other preference parameters are the utility discount factor $\beta = 0.96$ (as in Cocco et al., 2005), and the parameter capturing the strength of the bequest motive b = 2.5 (as in Gomes and Michaelides, 2005), which bears the interpretation of the number of years of her descendants' consumption that the investor intends to save for.

⁵ For the high school group, the variances of the permanent and transitory shocks (ω_t and ε_t respectively) are equal to $\sigma_{\omega}^2 = 0.0106$ and $\sigma_{\varepsilon}^2 = 0.0738$. The age-dependent trend is captured by a third-order polynomial in age fitted to the age coefficients estimates in Cocco et al. (2005), delivering a typical hump-shaped profile until retirement.

 $^{^{6}}$ Th policy functions for the risky portfolio share are shown and discussed in the online Appendix B.

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Table 1

Description	Parameter	Value	Source
Working life		20-65	Cocco et al. (2005)
Retirement		65-100	Cocco et al. (2005)
Risk aversion	γ	5	Chang et al. (2018)
Replacement ratio	λ	0.68	OECD (2015)
Discount factor	β	0.96	Cocco et al. (2005)
Bequest Motive	b	2.5	Gomes and Michaelides (2005)
Variance of permanent shocks to labor income	$\sigma^2_\omega \ \sigma^2_\epsilon$	0.0106	Cocco et al. (2005)
Variance of transitory shocks to labor income	σ_{ϵ}^2	0.0738	Cocco et al. (2005)
Riskless rate	r	2%	Cocco et al. (2005)
Excess returns on stocks	μ^{s}	4%	Cocco et al. (2005)
Variance of stock returns innovations	σ_s^2	0.025	Cocco et al. (2005)
Stock ret./permanent lab. income shock correlation	ρ_{sY}	0	Cocco et al. (2005)
Unemployment benefits			
Short-term unemployed	ξ1	0.3	OECD (2010)
Long-term unemployed	ξ2	0.1	OECD (2010)
Human Capital Loss	-		
Short-term unemployed	Ψ_1	0	
Long-term unemployed	Ψ_2	0.25	Jacobson et al. (1993)

This table reports benchmark values of relevant parameters with source references.

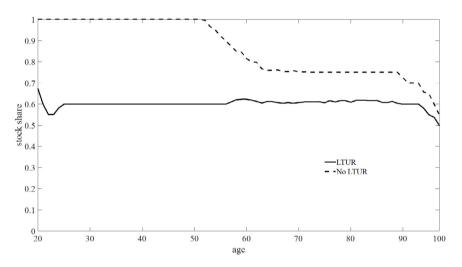


Fig. 1. Optimal life-cycle stock share profiles. This figure displays the median of the distribution of simulated stock investment life-cycle profiles for individuals of age 20 to 100 in the case of long-term unemployment risk (LTUR, black lines), and No long-term unemployment risk (No LTUR, grey lines).

investment over the whole working life. Moreover, as workers grow older, two offsetting effects are at work. First, the standard hedge effect of the decrease in human capital over time causes a reduction in the optimal stock portfolio share. Second, as the worker safely comes close to retirement, the risk of longterm unemployment falls, thereby reducing the uncertainty on future labor (and pension) incomes. Overall, the resolution of uncertainty compensates the hedge effect, making the optimal risky portfolio share relatively flat over the life cycle. Therefore, introducing long-term unemployment risk with human capital loss not only reduces the level of stock investment, but also alters substantially its life-cycle profile, departing from the conventional wisdom pointing to a larger risky investment when young and a gradual shift to more conservative portfolios over time.

Examination of the distribution of the optimal stock share across individuals shows that the introduction of permanent consequences of long-term unemployment shrinks the heterogeneity of optimal portfolio choices across agents characterized by different employment histories. Along most of the working life, a large portion of the distribution is closely gathered around the median allocation, and the dispersion of optimal shares increases only near retirement and remains constant thereafter. The similarity of portfolio choices of a large number of investors is due to the shape of the optimal policy functions, that are relatively flat for a wide range of wealth levels, implying that even sizeable differences in the amount of accumulated wealth result in homogeneous asset allocation choices.⁷

Overall, considering the risk of human capital losses due to the occurrence of (rare) long-term unemployment spells has important consequences for optimal life-cycle asset allocation: a lower portfolio share invested in risky assets (even with a moderate degree of risk aversion), with a remarkably flat age profile. This is in sharp contrast with the implications of the standard life-cycle model embodied in the popular financial advice of a high stock exposure when young, steadily decreasing with age. Our main results are robust to a wide range of changes in parameter calibration and extensions of the model. Bagliano et al. (2019) show that the flat stock investment profile obtains also when the human capital loss due to long-term unemployment (captured by Ψ_2) is reduced from 25% to 15% of previous permanent labor incomes and the probability of entering long-term unemployment $(\pi_{u_1u_2})$ is decreased from 15% to 10%. The same conclusion applies when long-term unemployment risk is modeled as age-dependent, being lower for younger workers and increasing with age. Similarly, changes in the degree of risk aversion (γ) affect only the average

 $^{^{7}\,}$ Online Appendix B shows policy functions for the risky portfolio share at various ages.

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level but not the flat age profile of stock investment, which is also preserved during the whole working life when the utility discount factor (β) is substantially reduced from 0.96 to 0.85. In addition, Appendix C shows that adopting Epstein–Zin preferences (whereby the elasticity of intertemporal substitution can be set independently of the degree of risk aversion) and assuming a positive correlation between stock return and labor income innovations do not substantially alter the flatness of the risky share age profile, only reducing its level during working life in the latter case. The same conclusion applies when we allow for correlation between unemployment risk and financial risk due to the dependence of both unemployment probabilities and stock return innovations on a common aggregate factor, namely the state of the business cycle. Overall, the preceding experiments confirm the robustness of our results, pointing to the relevance of the human capital loss effect in shaping optimal life-cycle asset allocation choices.

4. Welfare analysis

The main features of optimal stock investment obtained from standard life-cycle models of asset allocation are embodied in simple investment rules proposed by pension funds and other institutional investors and in popular financial advice. Those rules broadly share the distinctive features of a large stock share for young workers (often in excess of 80%), declining gradually to a more modest level when investors approach retirement. For example, Vanguard's long-run investment strategy is explicitly based on the results of standard life-cycle models: "The majority of younger individuals' ultimate retirement wealth is in the form of what they will earn in the future, or their human capital. Therefore, it may be appropriate for a younger person's portfolio to have a large committment to stocks to balance and diversify his or her risk exposure to work-related earnings (Viceira, 2001; Cocco et al., 2005). ... [E]quity allocations should decline with age to help manage risk through time". (Vanguard, 2019, p. 3). The welfare loss associated with the adoption of simple "rules of thumb" instead of the optimal life-cycle profile is typically low and comparable to a lifetime reduction of the investor's annual consumption level in the range of 0.2-0.8% (Cocco et al., 2005; Love, 2013).⁸

As shown in the previous section, when the possibility of longterm unemployment with human capital loss is allowed for, the resulting optimal age profile of stock investment is remarkably different: the risky portfolio share is lower on average during working life and relatively flat along the whole life cycle. This section provides a quantitative assessment of the welfare loss incurred by agents who follow simple portfolio allocation rules related to age in this alternative environment. In particular, we compare the optimal asset allocation policy, displayed in Fig. 2 as the solid line, with two suboptimal investment rules related to the investor's age.

The first is the typical "age rule", frequently suggested by financial advisors, whereby the risky portfolio share is set at 100 less the investor's age. This age rule is depicted in Fig. 2 as the dashed straight line. The second rule of thumb is representative of the actual strategic asset allocation patterns adopted by Target Date Funds such as Vanguard (2019). As shown in Fig. 2 (dotted line), a high level of exposure to equity risk (90%) is maintained until the age of 40. Then, the stock share declines steadily over the remaining working life down to 50% at retirement (age 65) and is further reduced in the early retirement period to reach 30% at

age 72.⁹ This "Target Date Fund (*TDF*) rule" happens to be close to the optimal life-cycle risky investment profile in the absence of long-term unemployment risk.

The metric used to perform welfare comparisons is the standard consumption-equivalent (CE) variation.¹⁰ The CE variation is computed as the percentage increase in annual consumption an investor following a given rule of thumb would need to enjoy the same expected lifetime utility associated with the optimal asset allocation strategy.

In particular, when the agent chooses optimally consumption and the stock portfolio share, we obtain expected lifetime utility $V_{t_0}^*$ at the beginning of her working life (age 20) as:

$$V_{t_0}^* = E_{t_0} \left[\sum_{j=0}^T \beta^j \left(\prod_{k=-1}^{j-1} p_{t_0+k} \right) \frac{C_{t_0+j}^{*1-\gamma}}{1-\gamma} \right]$$
(8)

where $C_{t_0+j}^*$ denotes optimal consumption in period t_0+j . We convert this measure into consumption units by computing the constant consumption stream C^* that yields a discounted expected utility equal to $V_{t_0}^*$:

$$C^* = \left[\frac{(1-\gamma)V_{t_0}^*}{\sum_{j=0}^T \beta^j \left(\prod_{k=-1}^{j-1} p_{t_0+k}\right)}\right]^{\frac{1}{1-\gamma}}$$
(9)

Following the same procedure, when the investor maximizes utility using a rule of thumb for portfolio allocation (either the "age rule" or the "Target Date Fund rule"), we obtain the corresponding expected lifetime utility $V_{t_0}^R$ and the equivalent constant consumption stream C^R . Thus, the welfare cost $W_{t_0}^R$ for an investor at the beginning of her working life can be computed as the percentage loss in equivalent consumption suffered when she adopts an investment rule of thumb instead of the optimal strategy:

$$W_{t_0}^{R} = \frac{V^* \frac{1}{1-\gamma} - V^{R} \frac{1}{1-\gamma}}{V^{R} \frac{1}{1-\gamma}} = \frac{C^* - C^R}{C^R}$$
(10)

In practice, we simulate the discounted lifetime utility of 200.000 workers both under the optimal solution and under alternative simple investment rules of thumb, and use the averages across individuals to obtain a measure of the welfare loss according to (10).

Table 2 shows lifetime welfare losses, expressed in annual percentage CE variation, associated with the adoption of suboptimal rules of thumb in asset allocation. As a benchmark for comparison, the first row presents the welfare loss obtained when there is no unemployment risk,¹¹ as in the standard life-cycle setup of Cocco et al. (2005), and the optimal risky share is that displayed as the grey line in Fig. 1. In this environment, both the "age" and the "*TDF*" rules are relatively close to the optimal profile and the loss is rather small (0.55% and 0.18%, respectively), well in the range of other available results in the literature. When the risk of permanent decreases in earning prospects due to long-term unemployment is introduced in the model, the optimal age profile of the stock share changes substantially (see Fig. 2), and the associated welfare losses are much larger, as shown in the second row of Table 2. Adopting the "age rule" in managing portfolios

⁸ Larger welfare losses are obtained only when individuals can flexibly choose working hours and the age of retirement, and can invest in payout annuities beside stocks and bonds (Chai et al., 2011).

⁹ In Vanguard's Target Date Fund "glide path" asset allocation, the portfolio share not invested in (U.S. and international) stocks is invested in (U.S. and international) bonds and short-term Treasury Inflation-Protected Securities (Vanguard, 2019).

¹⁰ This metric is employed, among others, by Cocco et al. (2005), Chai et al. (2011), Winter et al. (2012) and Love (2013).

¹¹ All parameter values are calibrated as shown in Table 1.

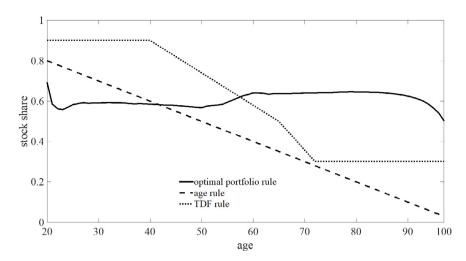


Fig. 2. Optimal and suboptimal life-cycle stock share profiles. This figure displays the optimal (average of 200.000) life cycle profiles (solid line), and suboptimal life cycle profiles (dashed line) for portfolio choice: "age rule"; dotted line: "Target Date Fund rule").

TDF

0.18

8.61

Table 2

wenare Losses.		
Expected Loss (%)	Age rule (100-age)	
No LTUR	0.55	
LTUR	2.94	

The table shows welfare losses, expressed in % of annual consumption, due to the adoption of suboptimal investment rules ("age rule" or "Target Date Fund rule") instead of the optimal strategy. In the first row, the optimal solution is obtained in the absence of long-term unemployment risk (No LTUR), whereas in the second row the risk of human capital loss following long-term unemployment is added to the model (LTUR).

entails a loss equivalent to around 3% of annual consumption, which increases up to 8.6% in the case of the "*TDF* rule".

Such sizeable welfare losses derive from the excess exposure to financial risk early in working life, and the under-exposure in retirement, embedded in the investment rules of thumb relative to the optimal strategy. This is particularly apparent in the case of the "TDF rule", which entails a stock share higher than optimal during almost all working life. The high risk of her financial portfolio (with a 90% stock share over the first two decades of working life) induces the investor to increase savings and wealth accumulation: consumption is therefore substantially lower than optimal over the first half of the working life, determining a sizeable decrease in expected utility that is not compensated by higher than optimal consumption levels over the remaining years of work and during retirement. Such distortion of the consumption and saving profile under the "TDF rule" yields a welfare loss three times larger than that under the "age rule", which entails more limited departures from the optimal intertemporal consumption pattern.

5. Conclusions

When a small risk of prolonged unemployment is considered, the (otherwise standard) model of life-cycle portfolio choice yields an optimal age profile of stock investment remarkably different from the popular, decreasing with age, pattern. In particular, the exposure to equity risk is much lower for young investors and relatively constant during working life and retirement. We show that in this case the welfare loss associated with the adoption of simple investment rules of thumb related to age is substantial, ranging from 3% to 9% of annual consumption. This result suggests a new design for pension plans offered by long-term investors, with a relatively constant equity exposure over the life cycle, suitable to effectively hedge the long-run consequences of long unemployment spells. Moreover, the reduced heterogeneity of the optimal risky share profile implies that relatively standard investment strategies may be appropriate for large classes of workers.

On a more general level, our analysis complements other results in the literature pointing to the relevance of extending life-cycle models of asset allocation to capture major features of labor market uncertainty, of which the risk of human capital loss due to long-term unemployment is one important dimension.

Appendix A. Supplementary data

Supplementary material related to this article can be found online at https://doi.org/10.1016/j.econlet.2020.109655.

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